

# CSC589 Introduction to Computer Vision Lecture 9

Sampling, Gaussian Pyramid

Bei Xiao

# What we have learned so far

- Image contrast, histograms, and basic manipulation
- Image Convolution
- Image Filters
- Fourier transform
- Filtering in Fourier transform

# What we want to achieve in this course?

- Basic image processing (extract contours, boundaries, edges).
- Basic understanding of image formation (camera models, projection)
- Basic skills of image synthesizing (textures, panorama images, image hybrid, stereo)
- Basic understanding of image features (HOG, SIFT, optical flow).
- Basic exposure of the state of the art computer vision applications. (multiple object tracking, segmentation, 3D construction, recognition of objects and faces)
- Application of machine learning in CV (Clustering, Bayesian, deep learning intro).
- Basic mathematical concepts behind image processing (Fourier transform, convolution, probability and statistics ).
- Brushing up numerical Python skills
- If you have made progress in at least 4 out of the above points, it is a success!

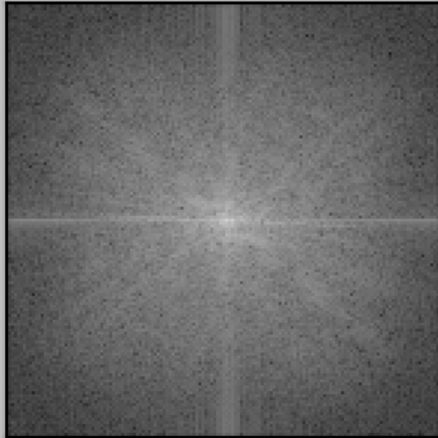
# Exercise 1

- Download the `FFTAnalysis.py` from blackboard.
- Use the `einstein.png`
- Right now the image removes low frequency (center) of the images.
- Can you modify the code that you are removing the high frequency (low pass) the image? You can do this either by directly modifying the DFT or use a filter.



# Exercise 1

Input Image



new Spectrum

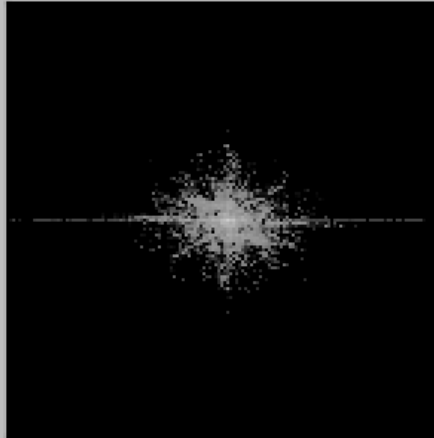
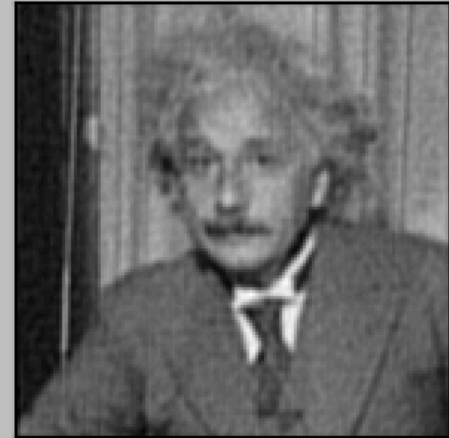


Image after LPF



```
mask = abs(fshift) < 10000  
fshift[mask]= 10
```

# Exercise 2

- Download the Cheetha and Zebra images
- DFT both images in Fourier domain and compute magnitude and phase. I have already did this in the helper code [PhaseandMagnitude.py](#)
- You can compute phase and magnitude as this:
  - `magnitude_zebra = 30*np.log(np.abs(fshift))`
  - `phase_zebra = np.angle(fshift)`
- Reconstruct the image with Cheetha phase and Zebra magnitude and vice versa. You have to do this yourself!

# Inverse Fourier Transform

- Forward Fourier:

```
img = misc.imread('cheetah.png',flatten=1)
f = np.fft.fft2(img)
fshift = np.fft.fftshift(f)
magnitude_cheetah = np.abs(fshift)
phase_cheetah = np.angle(fshift)
```

- Inverse Fourier:

```
re = magnitude_zebra*np.cos(phase_zebra)
im = magnitude_zebra*np.sin(phase_zebra)
F = re+1j*im
f_ishift = np.fft.ifftshift(F)
img_back = np.fft.ifft2(f_ishift)
img_back = np.abs(img_back)
#img_back= misc.bytescale(img_back)
print img_back.min(), img_back.max()
plt.imshow(np.uint8(img_back), cmap='gray')
```

# Filtering in frequency domain



FFT



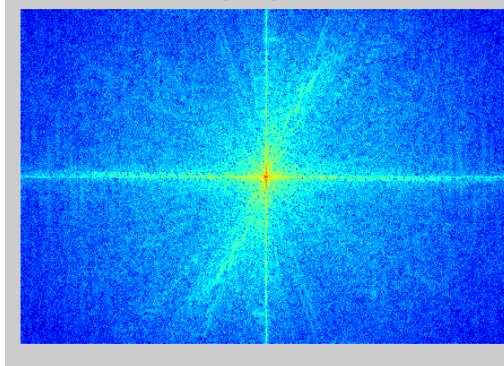
intensity image



FFT

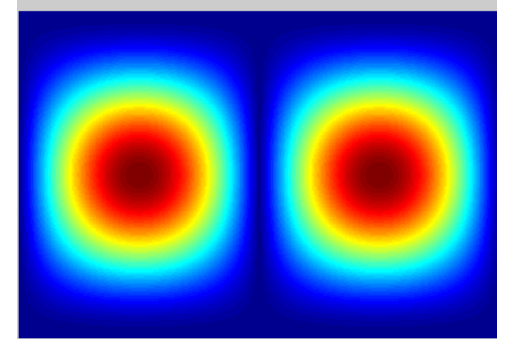


log fft magnitude

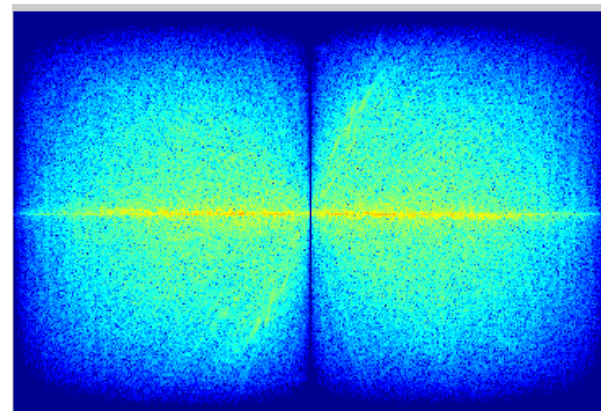


$\times$

$=$

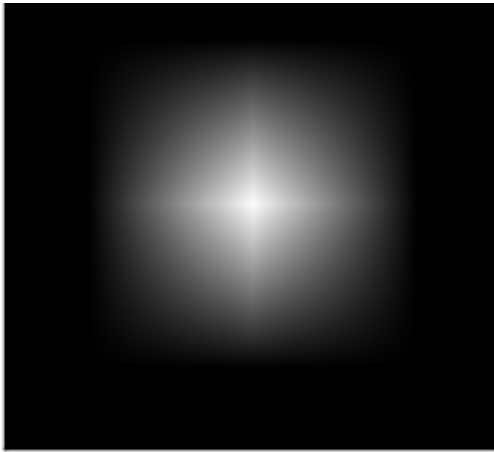


Inverse FFT

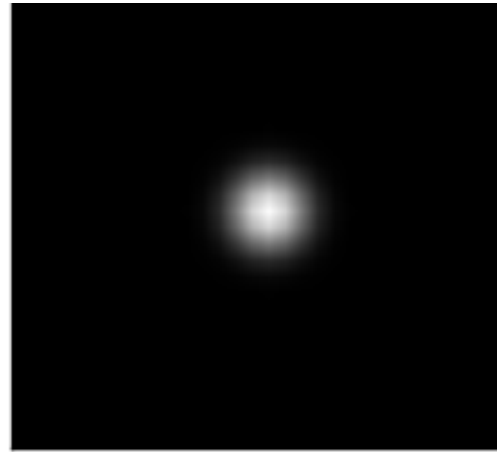


# Filters in Fourier Domain

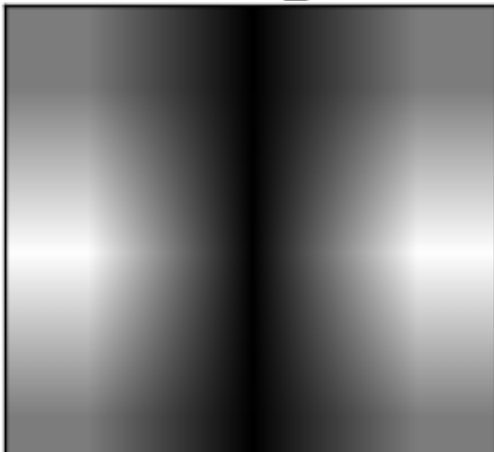
Mean filter



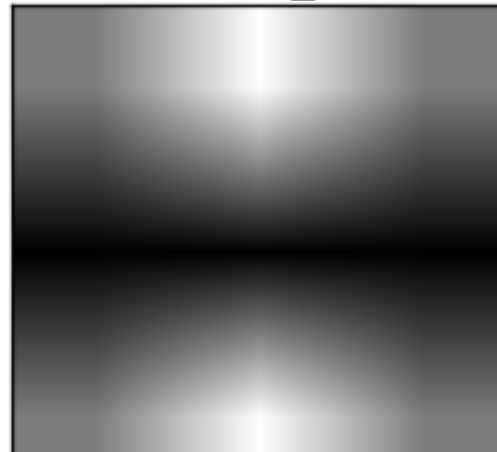
Gaussian Filter



sobel\_x

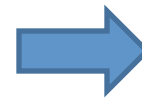


sobel\_y



# Sampling

**Why does a lower resolution image still make sense to us? What do we lose?**



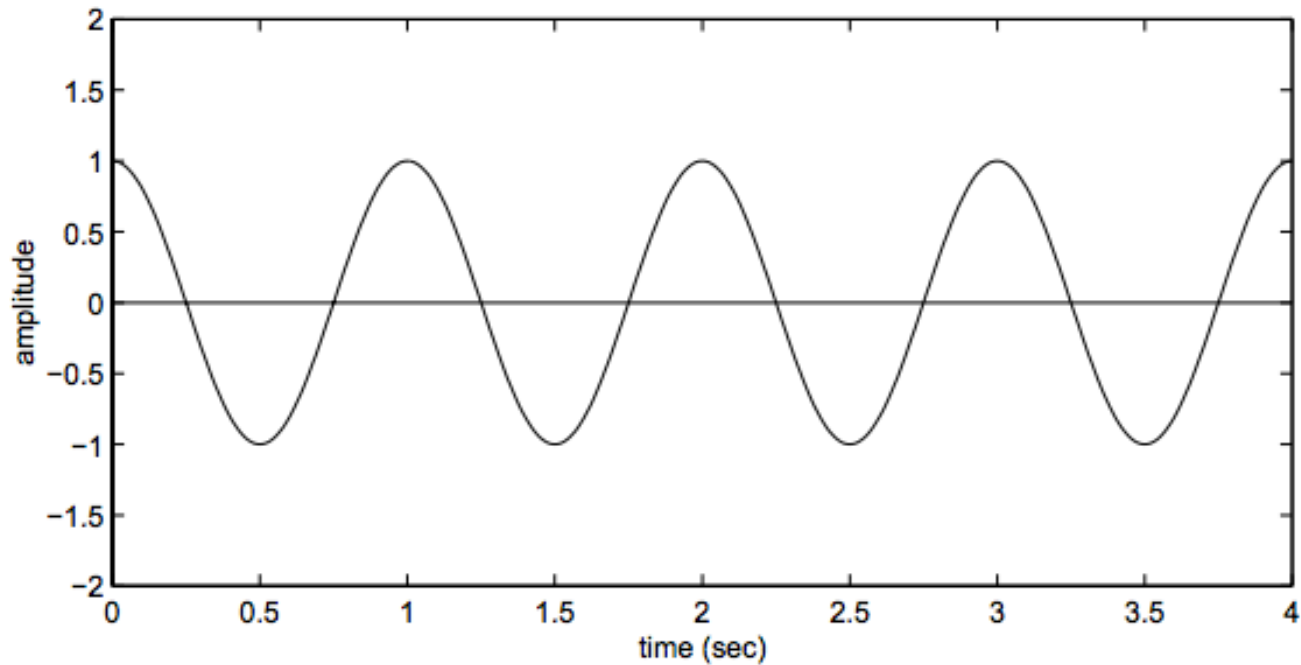
# Subsampling by a factor of 2



Throw away every other row and column to create a 1/2 size image

# Aliasing problem

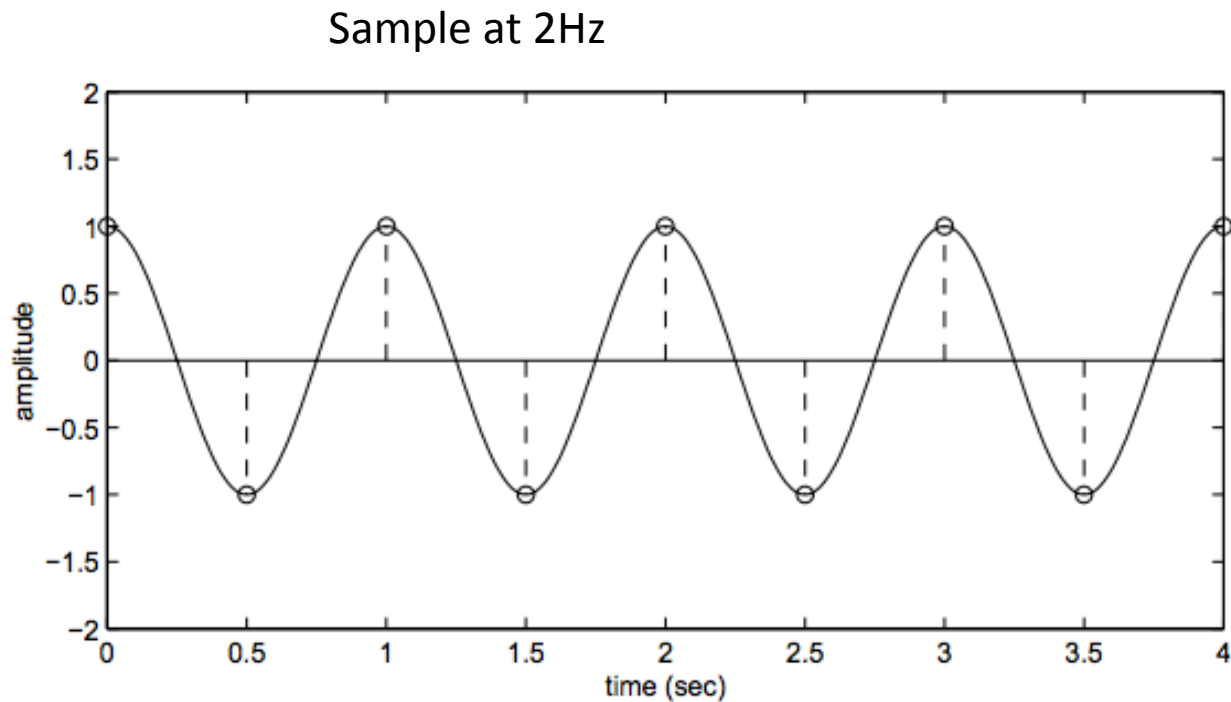
- 1D example (sinewave):





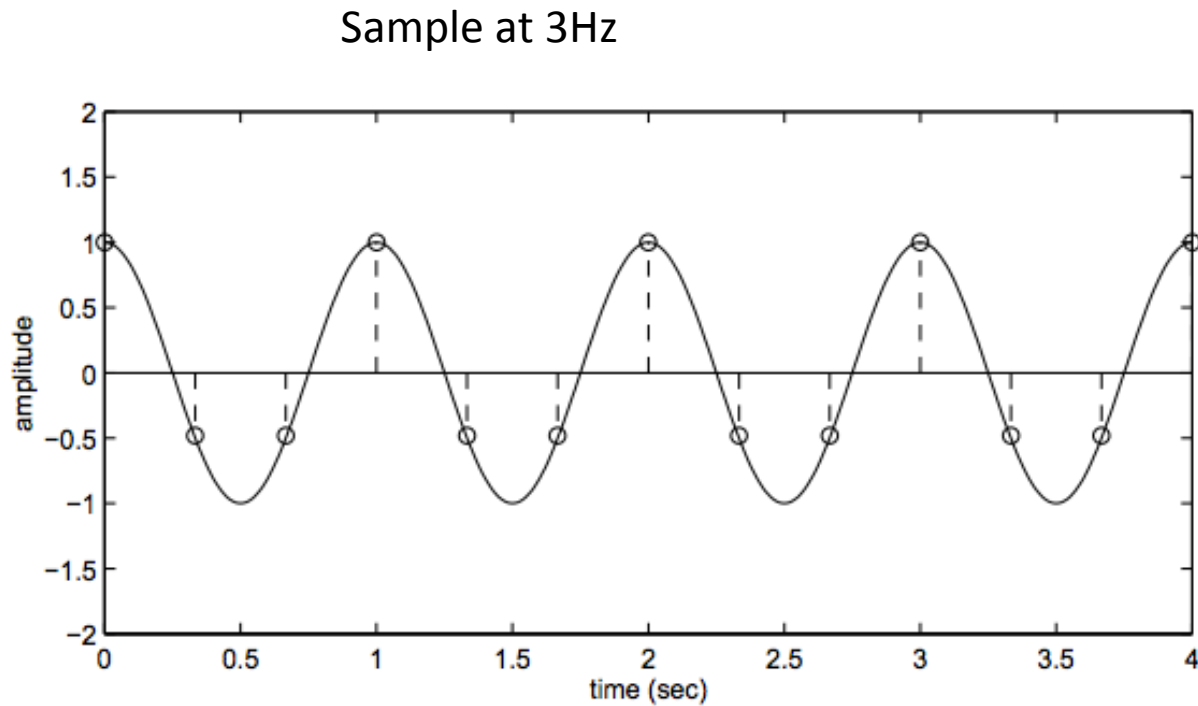
# Aliasing problem

- 1D example (sinewave):



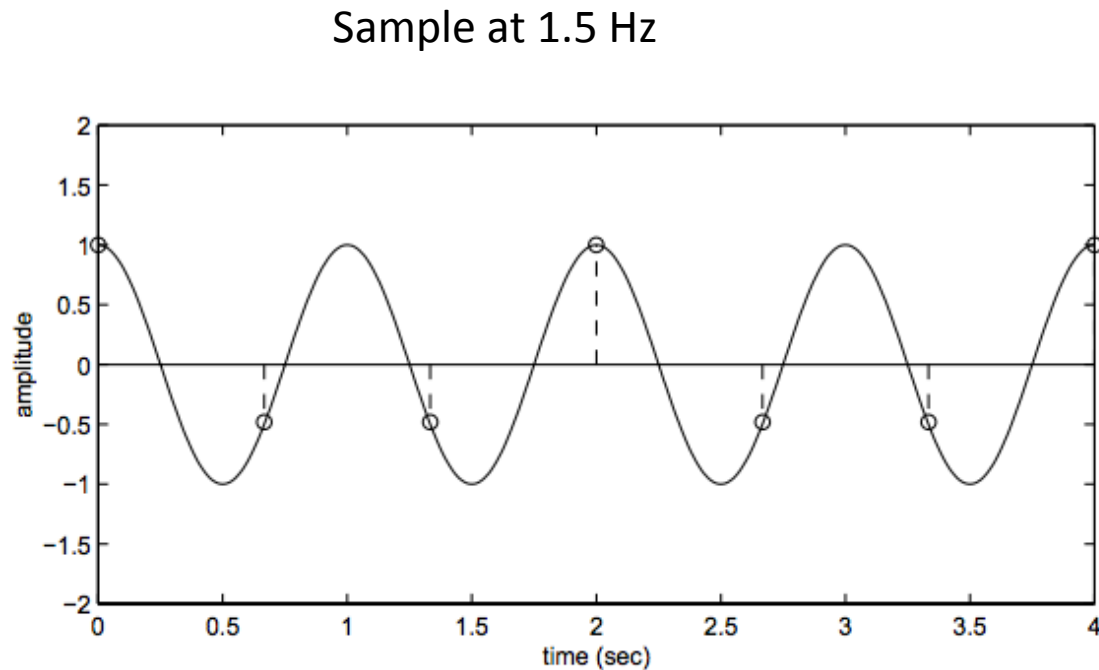
# Aliasing problem

- 1D example (sinewave):



# Aliasing problem

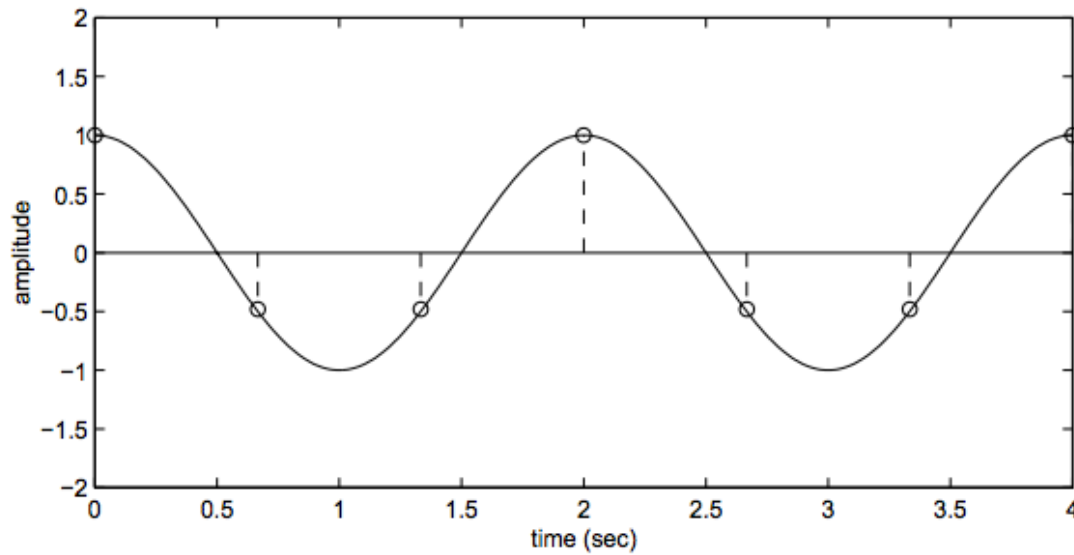
- 1D example (sinewave):



# Aliasing problem

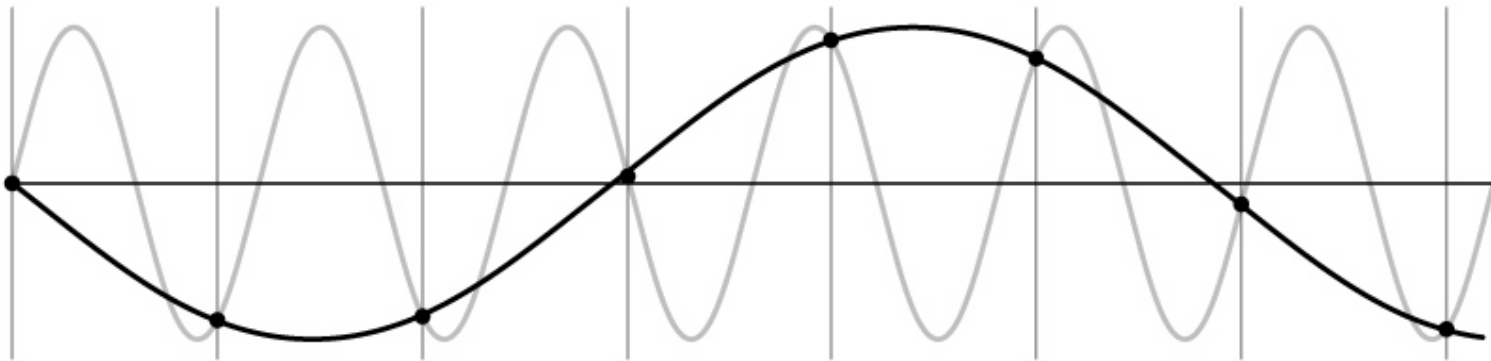
- 1D example (sinewave):

Sample at 1.5 Hz



# Aliasing problem

- 1D example (sinewave):



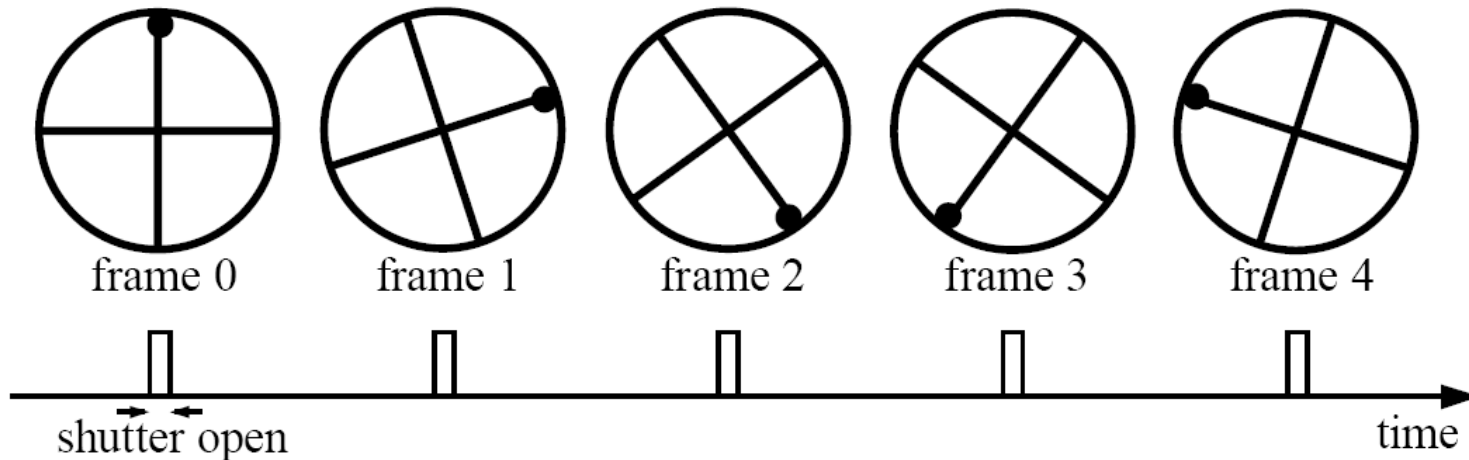
# Aliasing problem

- Sub-sampling may be dangerous....
- Characteristic errors may appear:
  - “Wagon wheels rolling the wrong way in movies”
  - “Checkerboards disintegrate in ray tracing”
  - “Striped shirts look funny on color television”

# Aliasing in video

Imagine a spoked wheel moving to the right (rotating clockwise).  
Mark wheel with dot so we can see what's happening.

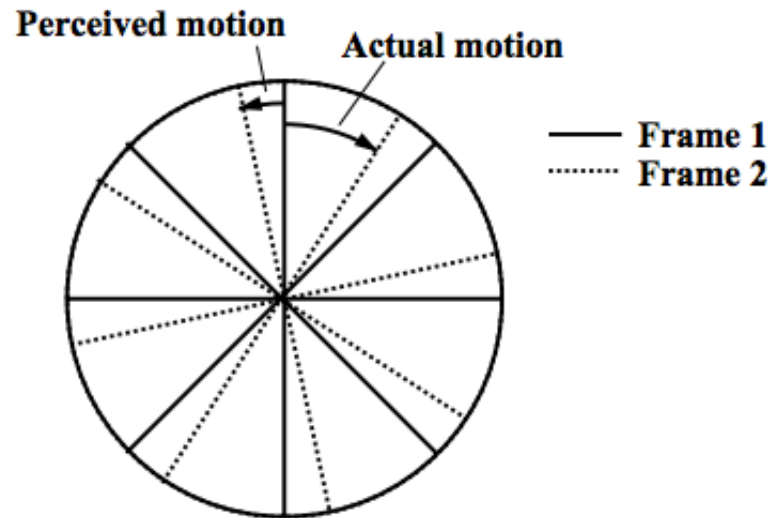
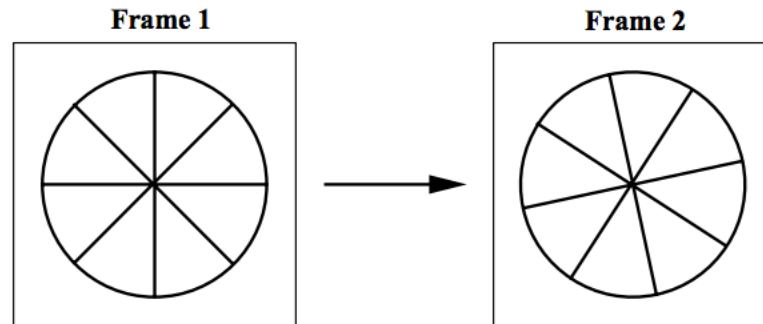
If camera shutter is only open for a fraction of a frame time (frame time = 1/30 sec. for video, 1/24 sec. for film):



Without dot, wheel appears to be rotating slowly backwards!  
(counterclockwise)

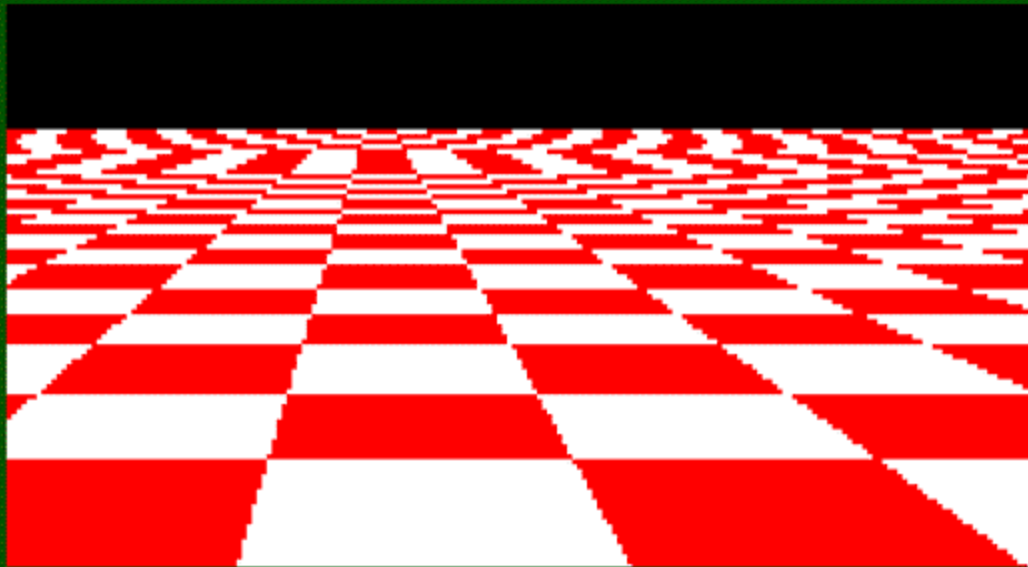
Visual illusion: <http://www.michaelbach.de/ot/mot-wagonWheel/index.html>

# Aliasing in video





# Aliasing in graphics



**Disintegrating textures**

# Sampling and aliasing

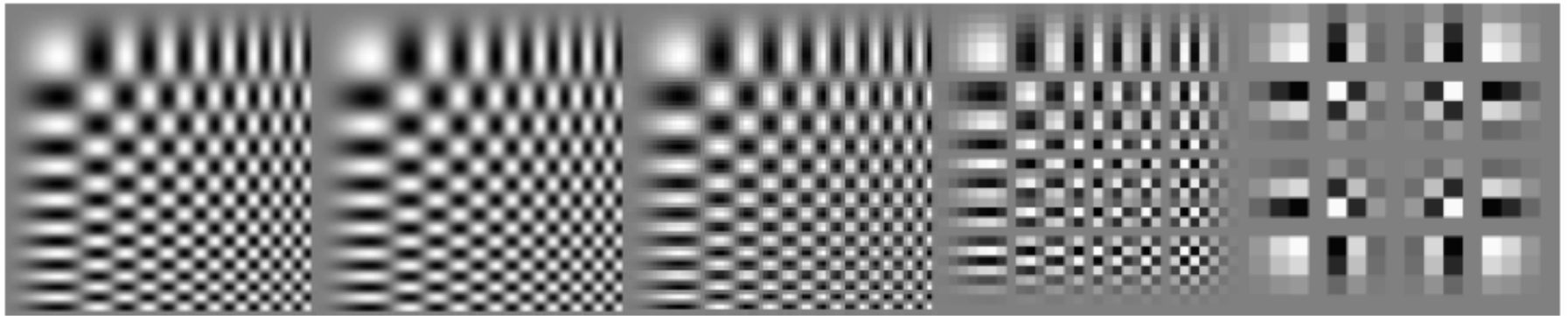
256x256

128x128

64x64

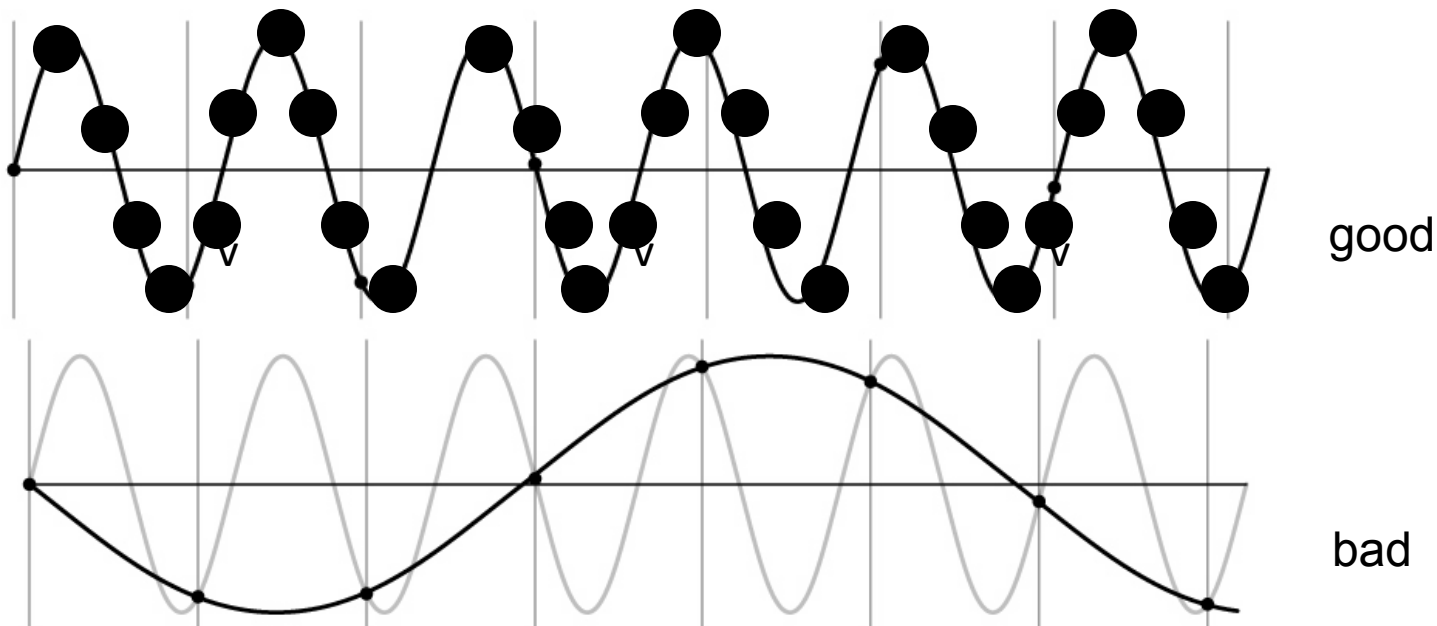
32x32

16x16



# Nyquist-Shannon Sampling Theorem

- When sampling a signal at discrete intervals, the sampling frequency must be  $\geq 2 \times f_{\max}$
- $f_{\max}$  = max frequency of the input signal
- This will allow to reconstruct the original perfectly from the sampled version



# Anti-aliasing

## Solutions:

- Sample more often
- Get rid of all frequencies that are greater than half the new sampling frequency
  - Will lose information
  - But it's better than aliasing
  - Apply a smoothing filter

# Algorithm for downsampling by factor of 2

1. Start with image(h, w)

2. Apply low-pass filter

```
im_blur = ndimage.filters.gaussian_filter(image, 7)
```

3. Sample every other pixel

```
im_small = im_blur[::2; ::2];
```

# Text images

Welcome to Joe's webpage!  $\xrightarrow{\text{subsampling}}$  Welcome to Joe's webpage!

Welcome to Joe's webpage!  $\xrightarrow{\text{smoothing}}$  Welcome to Joe's webpage!

$\downarrow$  subsampling

Welcome to Joe's webpage!

# Anti-aliasing

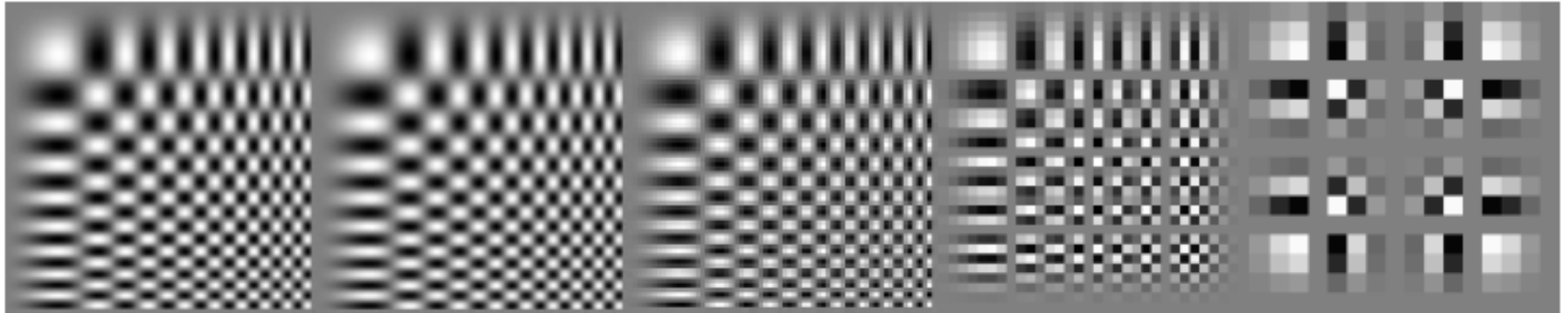
256x256

128x128

64x64

32x32

16x16



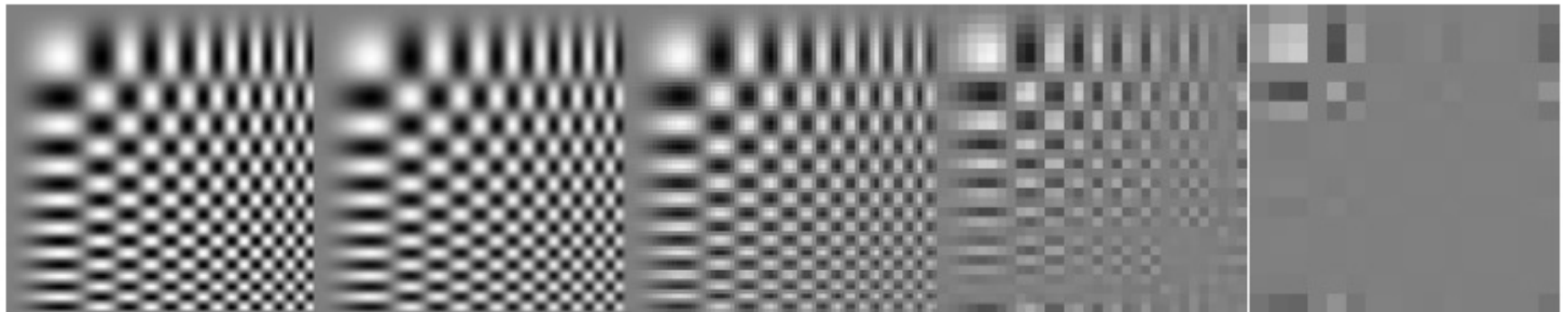
256x256

128x128

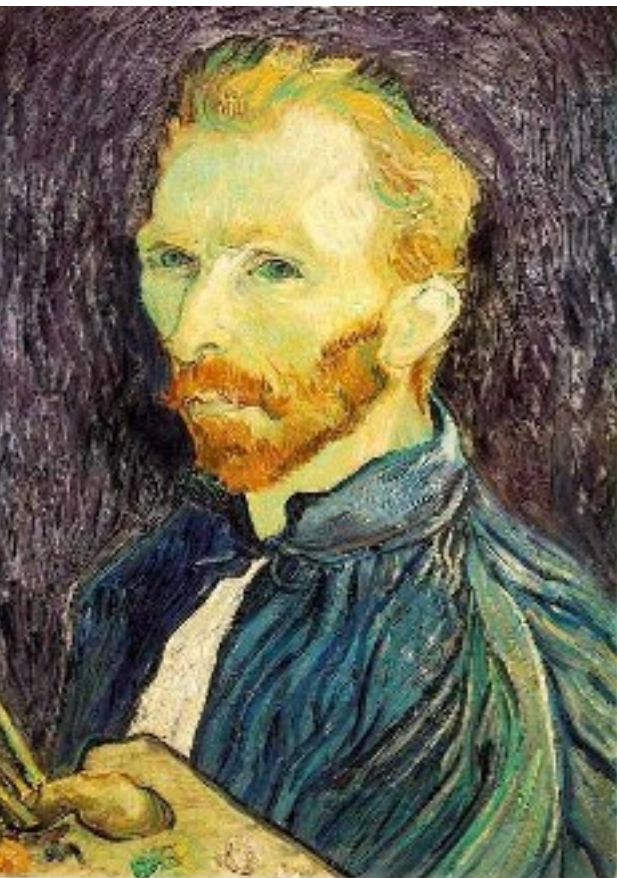
64x64

32x32

16x16



# Subsampling without pre-filtering



1/2



1/4 (2x zoom)



1/8 (4x zoom)



# Subsampling with Gaussian pre-filtering



Gaussian  $1/2$

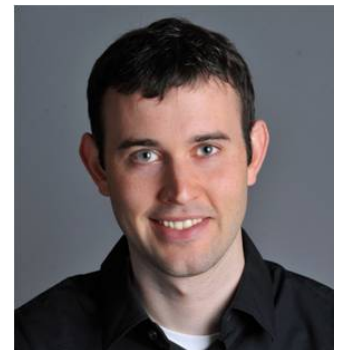
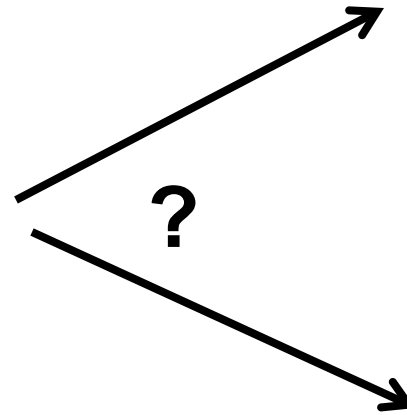


G  $1/4$



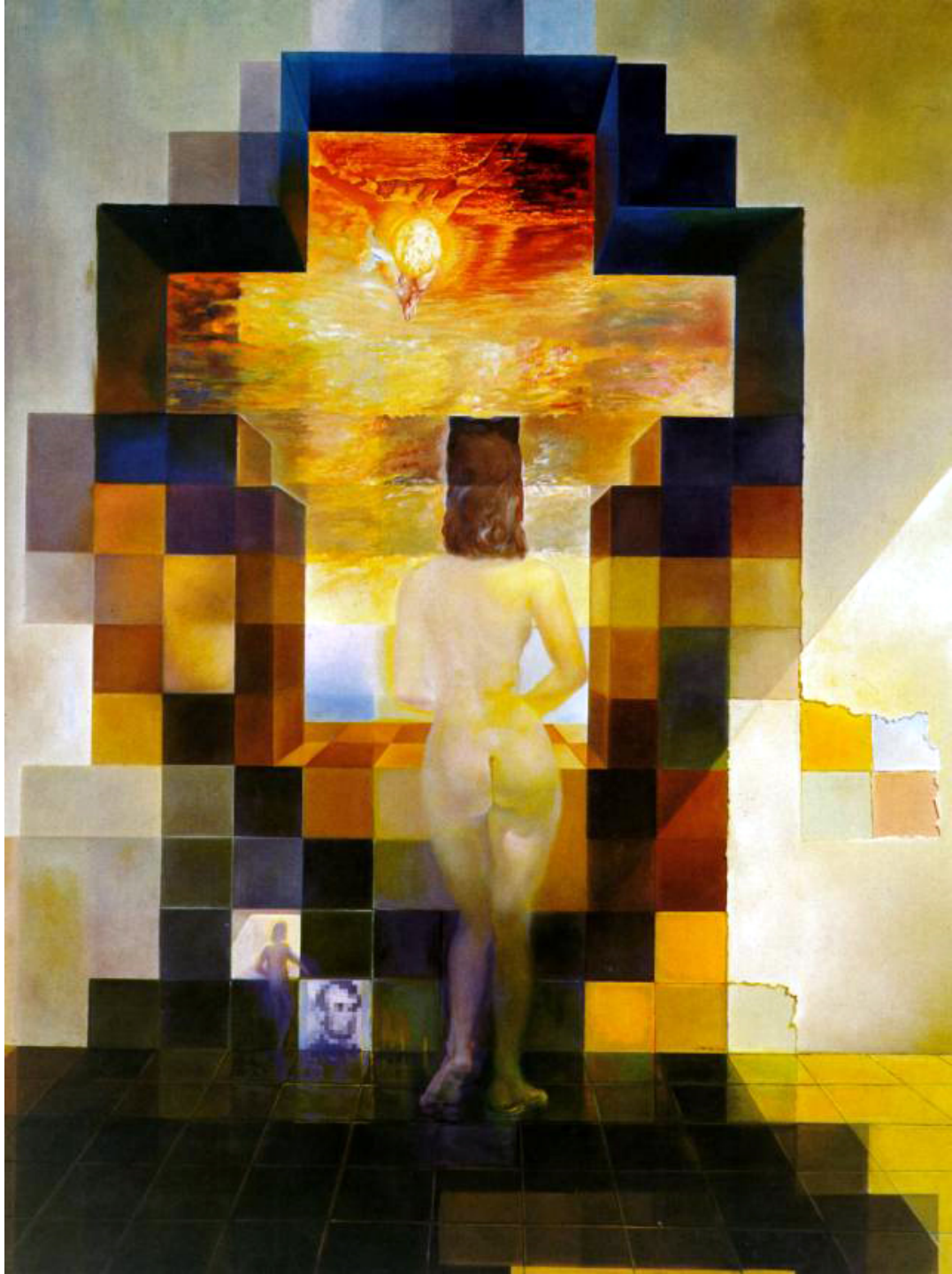
G  $1/8$

# Why do we get different, distance-dependent interpretations of hybrid images?



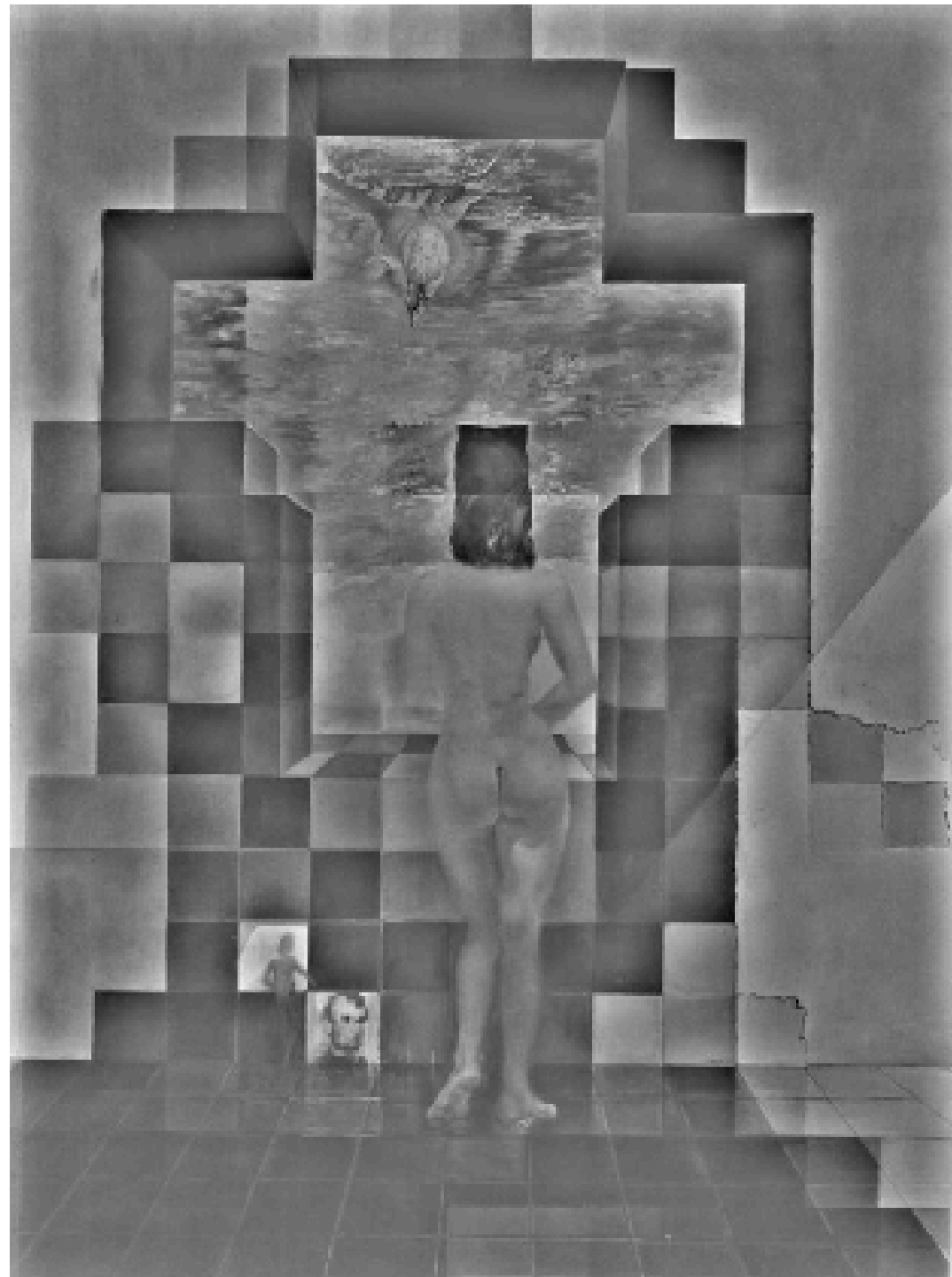
Salvador Dali invented Hybrid Images?

Salvador Dali  
*"Gala Contemplating the Mediterranean Sea, which at 30 meters becomes the portrait of Abraham Lincoln"*, 1976

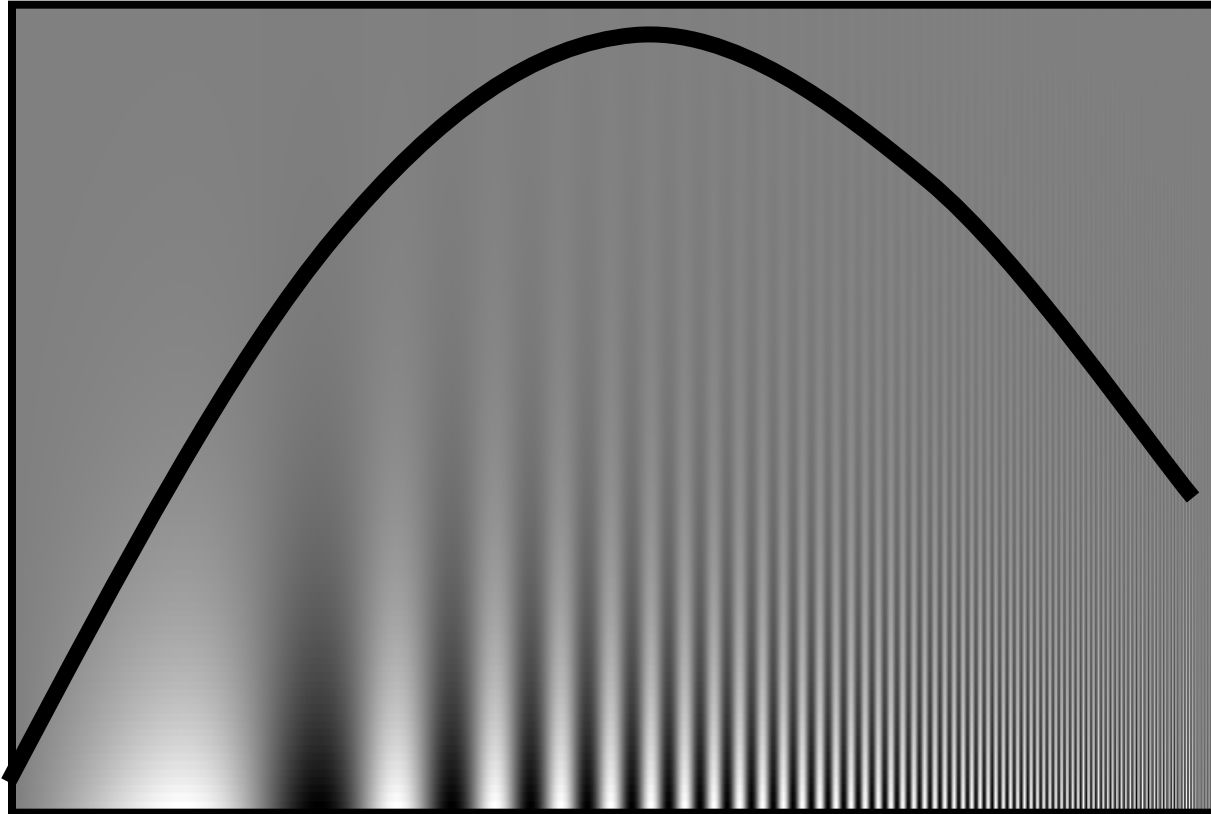






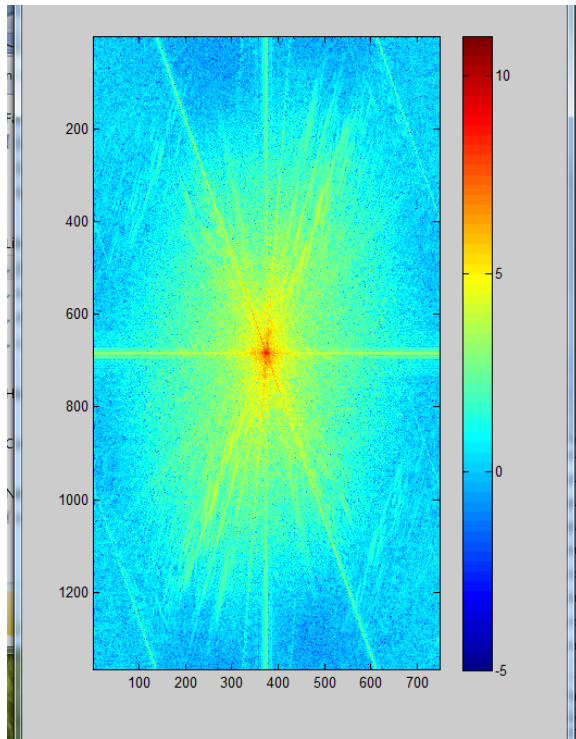


# Campbell-Robson contrast sensitivity curve

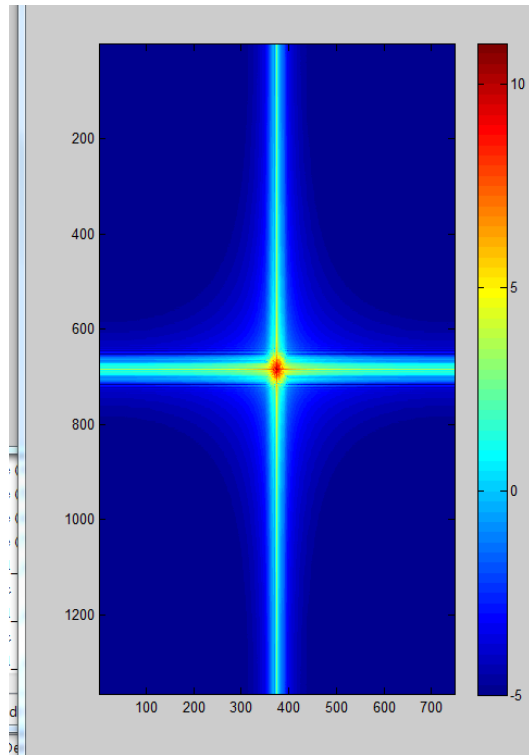


# Hybrid Image in FFT

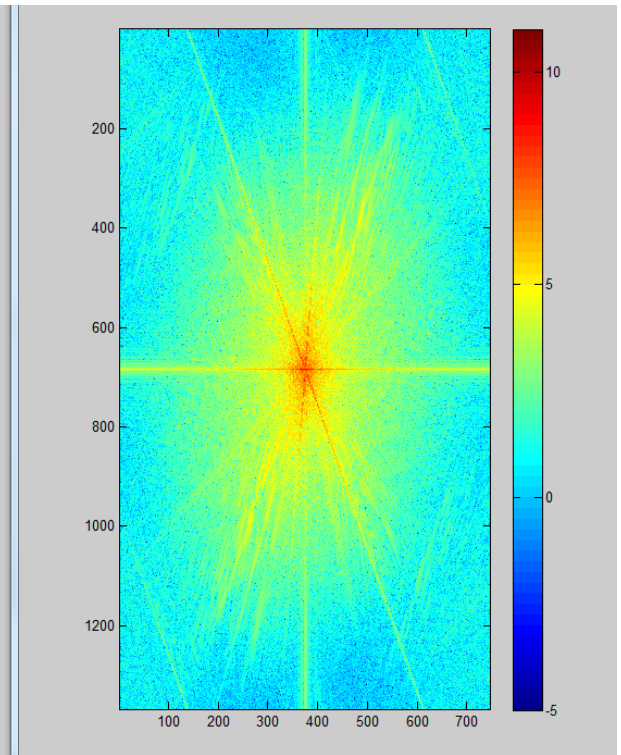
Hybrid Image



Low-passed Image

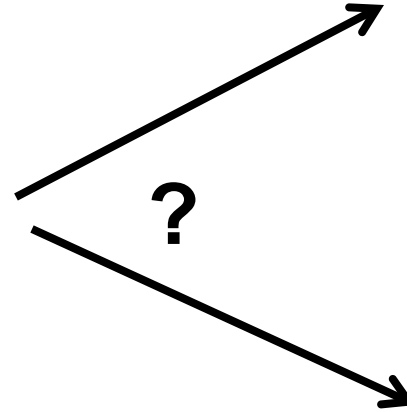


High-passed Image



# Perception

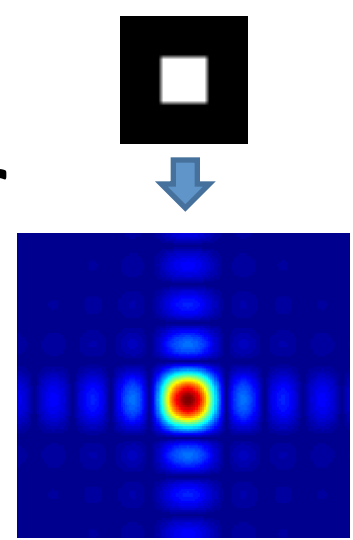
**Why do we get different, distance-dependent interpretations of hybrid images?**





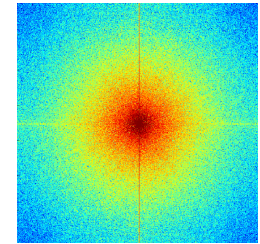
# Things to Remember

- Sometimes it makes sense to think of images and filtering in the frequency domain
  - Fourier analysis

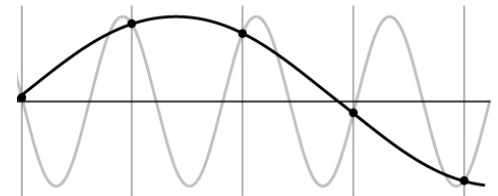


- Can be faster to filter using FFT for large images ( $N \log N$  vs.  $N^2$  for auto-correlation)

- Images are mostly smooth
  - Basis for compression

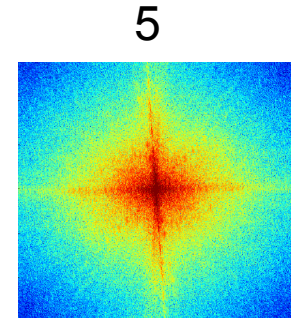
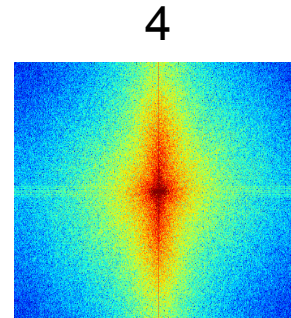
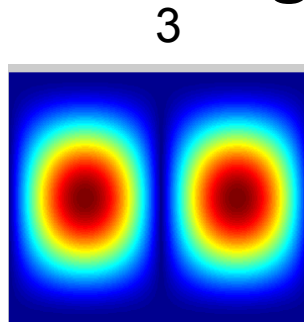
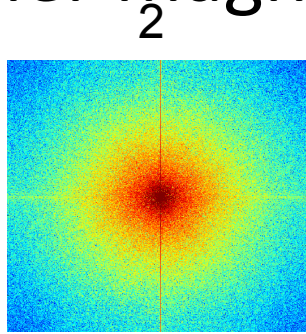
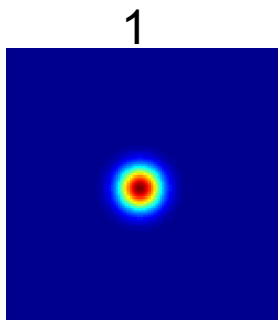


- Remember to low-pass before sampling



# Practice question

1. Match the spatial domain image to the Fourier magnitude image

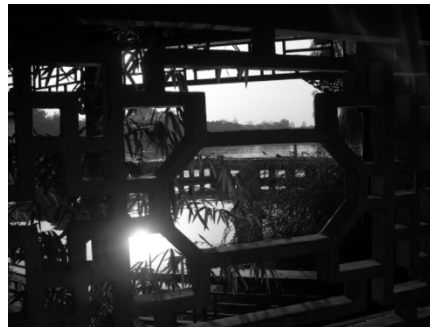


B

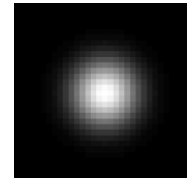
A



C



D



E



# Take home reading

- Aliasing  
<http://redwood.berkeley.edu/bruno/npb261/aliasing.pdf>
- Fourier Transform: Chapter 3.4
- Next class: Template Matching, Gaussian Pyramid, Filter banks and Texture